

Searches for Lepton Flavour Violation and Lepton Number Violation in Hadron Decays

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on behalf of the LHCb collaboration
including results from the B factories

Heidelberg University

Flavour Physics and CP Violation 2012

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Outline

1 Lepton Number Violation

- $D^- \rightarrow \pi^+ / K^+ \ell^- \ell^-$
- $B^- \rightarrow h^+ \ell^- \ell^-$
- $B^- \rightarrow D^0 \pi^+ \mu^- \mu^-$

2 Lepton Flavour Violation

- $D^- \rightarrow h^- \ell^+ \ell'^-$
- $B^- \rightarrow \pi^- / K^- \tau^\pm \ell^\mp$

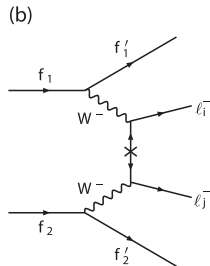
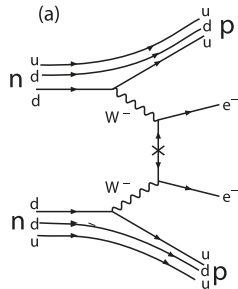
3 $\tau^- \rightarrow \mu^- \mu^- \mu^+$ at hadron colliders – first time shown!

Lepton Number Violation

- $D^- \rightarrow \pi^+ / K^+ \ell^- \ell^-$
- $B^- \rightarrow h^+ \ell^- \ell^-$
- $B^- \rightarrow D^0 \pi^+ \mu^- \mu^-$

Lepton Number Violation

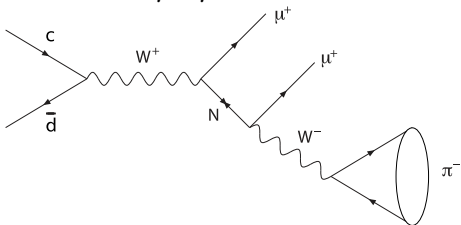
- Lepton number is conserved in the Standard Model
- Lepton number violation introduced in many New Physics models, e. g.:
 - 4th quark generation
([arXiv:hep-ph/1106.0343](https://arxiv.org/abs/hep-ph/1106.0343))
 - SO(10) SUSY GUT
([arXiv:hep-ph/9501298](https://arxiv.org/abs/hep-ph/9501298))
 - exotic Higgs
(A. Zee, *Phys. Lett. B* **93**, 389 (1980))
- Majorana neutrinos violate Lepton Number
classic search: neutrinoless double beta-decay
(→ [Dongming Mei's talk](#))
- Similar fundamental process with mesons





LNV in meson decays

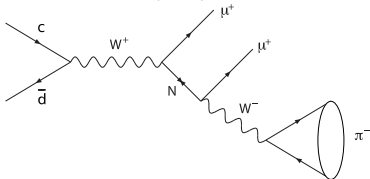
$$D^+ \rightarrow \pi^- \mu^+ \mu^+$$



- resonant production in accessible mass range
- rates depend on Majorana neutrino–lepton coupling $|V_{\mu 4}|$ (e.g. [arXiv:0901.3589](https://arxiv.org/abs/0901.3589))
- $m_4 = m_{\ell^-, \pi^+}$

LNV in meson decays

$$D^+ \rightarrow \pi^- \mu^+ \mu^+$$

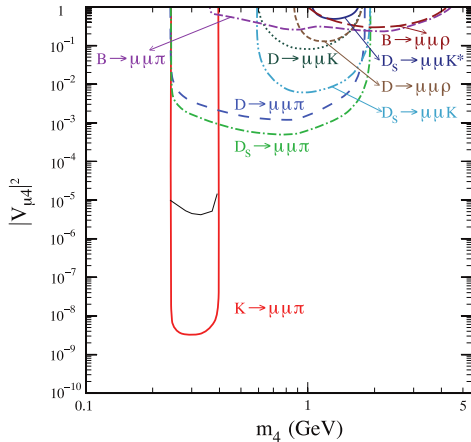


- resonant production in accessible mass range
- rates depend on Majorana neutrino-lepton coupling

$$|V_{\mu 4}|$$

(e.g. [arXiv:0901.3589](https://arxiv.org/abs/0901.3589))

- $m_4 = m_{\ell^-, \pi^+}$



Status of 2009

[arXiv:0901.3589](https://arxiv.org/abs/0901.3589)



limits on LNV in charm decays

charm decays

- latest limits from BaBar
- includes Lepton Number and Flavour Violation
- comprehensive list of D^+ , D_s^+ , and Λ_c^+ decays



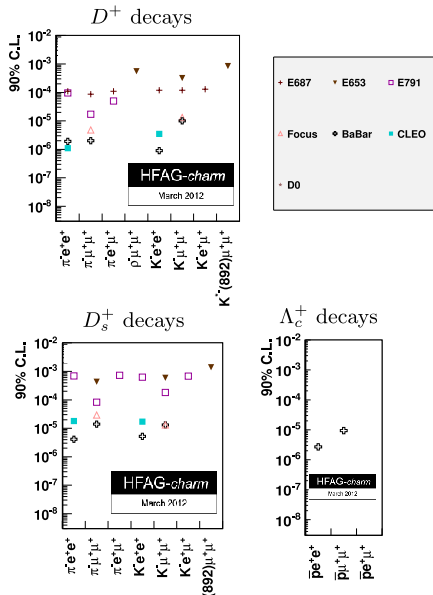
Decay mode	Yield (events)	Eff. (%)	BR UL	BF UL
			90% CL (10^{-4})	90% CL (10^{-6})
$D^+ \rightarrow \pi^- e^+ e^+$	$4.7 \pm 4.7 \pm 0.5$	3.16	6.8	1.9
$D^+ \rightarrow \pi^- \mu^+ \mu^+$	$-3.1 \pm 1.2 \pm 0.5$	0.70	7.5	2.0
$D^+ \rightarrow \pi^- \mu^+ e^+$	$-5.1 \pm 4.2 \pm 2.0$	1.72	7.4	2.0
$D_s^+ \rightarrow \pi^- e^+ e^+$	$-5.7 \pm 14. \pm 3.4$	6.84	1.8	4.1
$D_s^+ \rightarrow \pi^- \mu^+ \mu^+$	$0.6 \pm 5.1 \pm 2.7$	1.05	6.2	14
$D_s^+ \rightarrow \pi^- \mu^+ e^+$	$-0.2 \pm 7.9 \pm 0.6$	2.23	3.6	8.4
$D^+ \rightarrow K^- e^+ e^+$	$-2.8 \pm 2.4 \pm 0.2$	2.67	3.1	0.9
$D^+ \rightarrow K^- \mu^+ \mu^+$	$7.2 \pm 5.4 \pm 1.6$	0.80	37	10
$D^+ \rightarrow K^- \mu^+ e^+$	$-11.6 \pm 4.0 \pm 3.1$	1.52	6.8	1.9
$D_s^+ \rightarrow K^- e^+ e^+$	$2.3 \pm 7.9 \pm 3.3$	4.10	2.1	5.2
$D_s^+ \rightarrow K^- \mu^+ \mu^+$	$-2.3 \pm 5.0 \pm 2.8$	0.98	5.3	13
$D_s^+ \rightarrow K^- \mu^+ e^+$	$-14.0 \pm 8.4 \pm 2.0$	2.26	2.4	6.1
$\Lambda_c^+ \rightarrow \bar{p} e^+ e^+$	$-1.5 \pm 4.2 \pm 1.5$	5.14	0.4	2.7
$\Lambda_c^+ \rightarrow \bar{p} \mu^+ \mu^+$	$-0.0 \pm 2.1 \pm 0.6$	0.94	1.4	9.4
$\Lambda_c^+ \rightarrow \bar{p} \mu^+ e^+$	$10.1 \pm 5.8 \pm 3.5$	2.50	2.3	16

Phys. Rev. D **84**, 072006 (2011)

limits on LNV in charm decays

charm decays

- latest limits from BaBar
- includes Lepton Number and Flavour Violation
- comprehensive list of D^+ , D_s^+ , and Λ_c^+ decays
- best limit for most channels





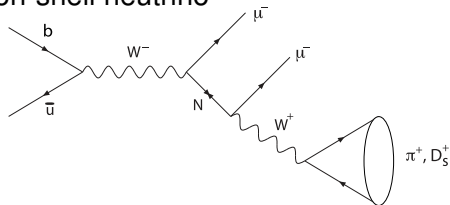
LVN in bottom decays

$$B^- \rightarrow h^+ \ell^- \ell^-$$

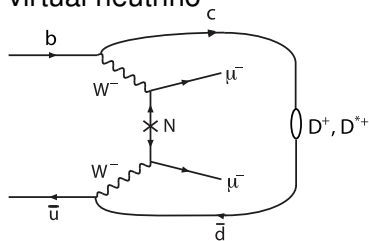


LNV in bottom decays

on-shell neutrino



virtual neutrino



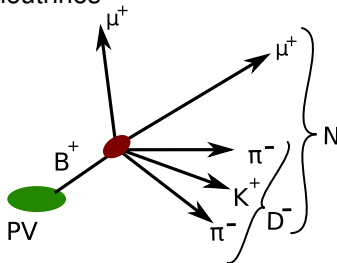
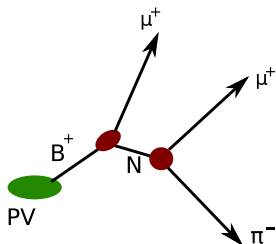
- resonant production in accessible mass range
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- $m_4 = m_{\ell^-, \pi^+}$

special for B decays

diagram without mass restriction
Cabbibo favoured for $B \rightarrow D$

search for Majorana neutrinos at LHCb

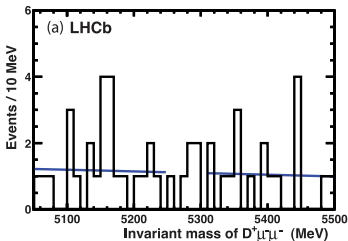
- searches at B factories in [Liang Sun's talk](#)
- LHCb: search for
 - $B^- \rightarrow \pi^+ \mu^- \mu^-$
 - $B^- \rightarrow D^+ \mu^- \mu^-$
 - $B^- \rightarrow D_s^+ \mu^- \mu^-$
 - $B^- \rightarrow D^{*+} \mu^- \mu^-$
- consider topology in reconstruction
 - allow for flight distance for on-shell neutrinos
 - common vertex for virtual neutrinos





virtual Majorana neutrinos

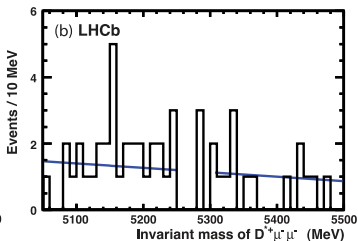
$$B^- \rightarrow D^+ \mu^- \mu^-$$



$$\mathcal{B}(B^- \rightarrow D^+ \mu^- \mu^-) < 6.9 \times 10^{-7}$$

@ 95% CL

$$B^- \rightarrow D^{*+} \mu^- \mu^-$$



$$\mathcal{B}(B^- \rightarrow D^{*+} \mu^- \mu^-) < 2.4 \times 10^{-6}$$

@ 95% CL

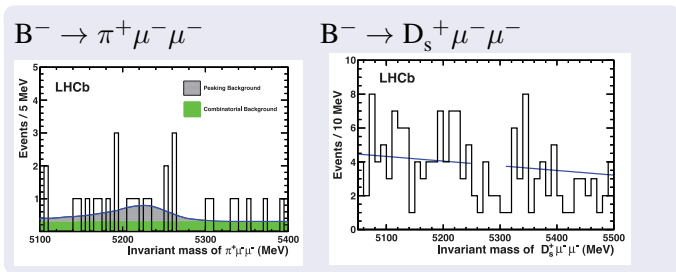
0.41 fb⁻¹

arXiv:1201.5600



on-shell Majorana neutrinos

- mis-identification rates from data with mass shape from simulation



assuming B^- phase space decay:

$$\mathcal{B}(B^- \rightarrow \pi^+ \mu^- \mu^-) < 1.3 \times 10^{-8}$$

@ 95% CL

$$\mathcal{B}(B^- \rightarrow D_s^+ \mu^- \mu^-) < 5.8 \times 10^{-7}$$

@ 95% CL



0.41 fb⁻¹

arXiv:1201.5600

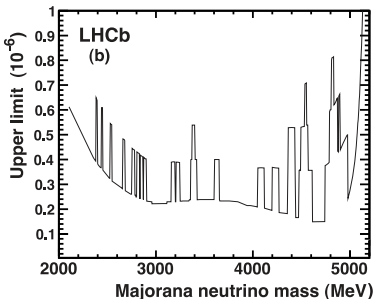
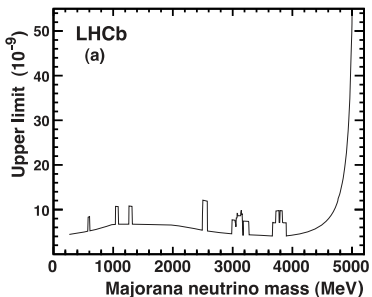
implications on Majorana mass

mass extraction

Determine limit as function of $h^+ \mu^-$ mass

$$B^- \rightarrow \pi^+ \mu^- \mu^-$$

$$B^- \rightarrow D_s^+ \mu^- \mu^-$$

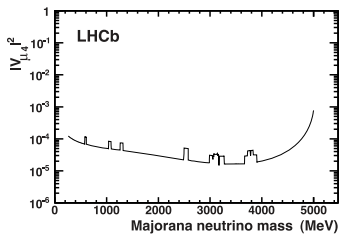


0.41 fb⁻¹

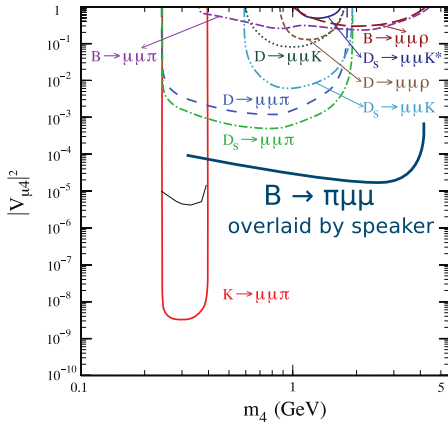
arXiv:1201.5600

new bounds for on shell Majorana neutrinos

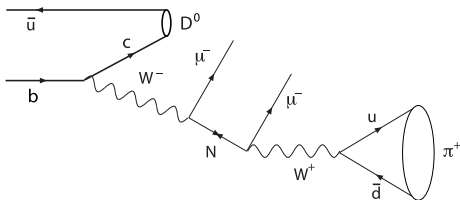
Status of 2009

LHCb limit on $|V_{\mu 4}|$ 

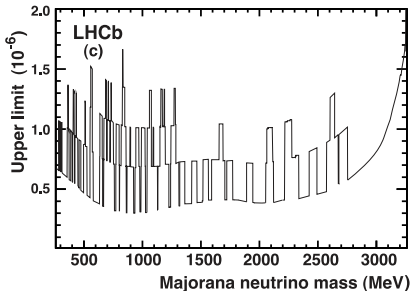
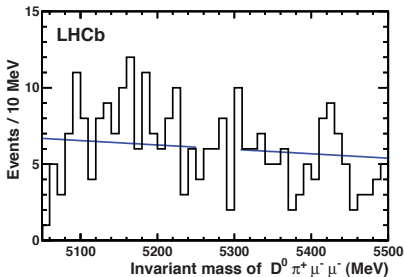
arXiv:1201.5600



arXiv:0901.3589



- Four body B decay complementary to three body decay ([arXiv:1108.6009](https://arxiv.org/abs/1108.6009))
- $m_4 = m(\pi^+ \mu^-)$
- + enhanced by W couplings
 - smaller mass range accessible ($260 \text{ MeV} < m_4 < 3.3 \text{ GeV}$)
- first performed at LHCb















$$\mathcal{B}(B^- \rightarrow D^0 \pi^+ \mu^- \mu^-) < 1.5 \times 10^{-6} \text{ @95\% CL }^a$$

Less restrictive than $B^- \rightarrow \pi^+ \mu^- \mu^-$ on $|V_{\mu 4}|^2$



^aLHCb, CERN-PH-EP-2012-006, [arXiv:1201.5600](https://arxiv.org/abs/1201.5600)

Summary on LNV in B decays

channel	limit		
$\mathcal{B}(B^- \rightarrow \pi^+ e^- e^-)$	$< 2.3 \times 10^{-8}$	@90 % CL	 ^a
$\mathcal{B}(B^- \rightarrow K^+ e^- e^-)$	$< 3.0 \times 10^{-8}$	@90 % CL	 ^a
$\mathcal{B}(B^- \rightarrow K^{*+} e^- e^-)$	$< 2.8 \times 10^{-6}$	@90 % CL	 ^b
$\mathcal{B}(B^- \rightarrow \rho^+ e^- e^-)$	$< 2.6 \times 10^{-6}$	@90 % CL	 ^b
$\mathcal{B}(B^- \rightarrow D^+ e^- e^-)$	$< 2.6 \times 10^{-6}$	@90 % CL	 ^c
$\mathcal{B}(B^- \rightarrow D^+ e^- \mu^-)$	$< 1.8 \times 10^{-6}$	@90 % CL	 ^c
$\mathcal{B}(B^- \rightarrow \pi^+ \mu^- \mu^-)$	$< 1.3 \times 10^{-8}$	@95 % CL	 ^d
$\mathcal{B}(B^- \rightarrow K^+ \mu^- \mu^-)$	$< 5.4 \times 10^{-7}$	@95 % CL	 ^e
$\mathcal{B}(B^- \rightarrow D^+ \mu^- \mu^-)$	$< 6.9 \times 10^{-7}$	@95 % CL	 ^d
$\mathcal{B}(B^- \rightarrow D^{*+} \mu^- \mu^-)$	$< 2.4 \times 10^{-6}$	@95 % CL	 ^d
$\mathcal{B}(B^- \rightarrow D_s^+ \mu^- \mu^-)$	$< 5.8 \times 10^{-7}$	@95 % CL	 ^d
$\mathcal{B}(B^- \rightarrow D^0 \pi^- \mu^- \mu^-)$	$< 1.5 \times 10^{-6}$	@95 % CL	 ^d

^aBaBar, *Phys. Rev. D* **85**, 071103 (2012)

^bCLEO, *Phys. Rev. D* **65**, 111102 (2002)

^cBelle, *Phys. Rev. D* **84**, 071106(R), (2011)

^dLHCb, CERN-PH-EP-2012-006, [arXiv:1201.5600](https://arxiv.org/abs/1201.5600) (2012)

^eLHCb, *Phys. Rev. Lett.* **108** 101601 (2012)

Lepton Flavour Violation

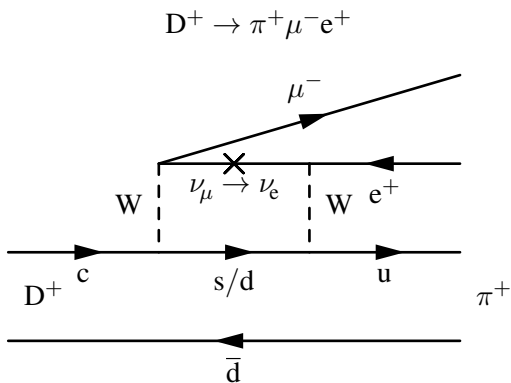
- $D^- \rightarrow h^- \ell^+ \ell'^-$
- $B^- \rightarrow \pi^- / K^- \tau^\pm \ell^\mp$
- $\tau^- \rightarrow \mu^- \mu^- \mu^+$



Lepton Flavour Violation

Standard Model + neutrino oscillation

- established for neutrinos
- can enter charged sector in loops
- predicted rates unmeasurable small





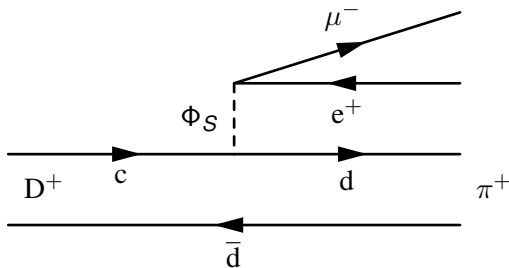
Lepton Flavour Violation

- established for neutrinos
- can enter charged sector in loops
- predicted rates unmeasurable small
- enhancement predicted in many New Physics models, e.g.
 - multi-Higgs extensions¹
 - leptoquarks²
 - low scale seesaw models³

¹Phys. Rev. D **44**, 1461²Z. Phys. C **61**, 613³Phys. Rev. D **73**, 074011

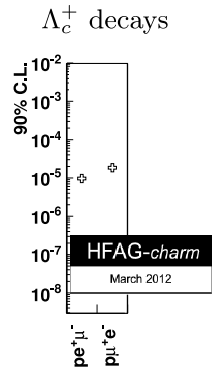
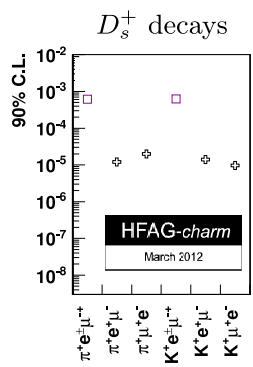
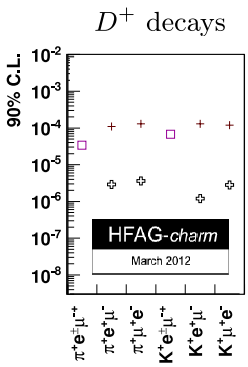
extended Higgs

$$D^+ \rightarrow \pi^+ \mu^- e^+$$





LFV in charm decays

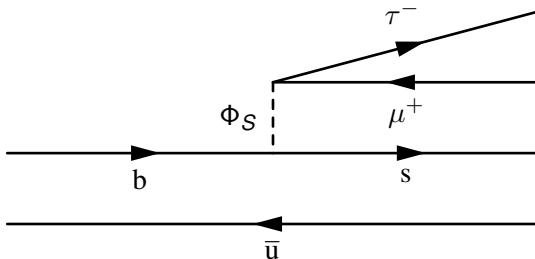


[HFAG]





LFV in bottom decays



- LFV τ sector not probed by D decays
- enough energy available in B decays
- multi Higgs models enhance $B \rightarrow h\tau\mu$ over other channels⁴
- challenging: neutrino in τ decay similar to $B \rightarrow X\ell\nu$

⁴Phys. Rev. D **44** 1461



LFV in bottom decays

channel	limit	
$\mathcal{B}(B^+ \rightarrow K^+ \tau^- \mu^+)$	$< 4.5 \times 10^{-5}$	a
$\mathcal{B}(B^+ \rightarrow K^+ \tau^+ \mu^-)$	$< 2.8 \times 10^{-5}$	a
$\mathcal{B}(B^+ \rightarrow K^+ \tau^- e^+)$	$< 4.3 \times 10^{-5}$	a
$\mathcal{B}(B^+ \rightarrow K^+ \tau^+ e^-)$	$< 1.5 \times 10^{-5}$	a
$\mathcal{B}(B^+ \rightarrow \pi^+ \tau^- \mu^+)$	$< 6.2 \times 10^{-5}$	a
$\mathcal{B}(B^+ \rightarrow \pi^+ \tau^+ \mu^-)$	$< 4.5 \times 10^{-5}$	a
$\mathcal{B}(B^+ \rightarrow \pi^+ \tau^- e^+)$	$< 7.4 \times 10^{-5}$	a
$\mathcal{B}(B^+ \rightarrow \pi^+ \tau^+ e^-)$	$< 2.0 \times 10^{-5}$	a
$\mathcal{B}(B^+ \rightarrow \pi^+ \mu^\pm e^\mp)$	$< 1.7 \times 10^{-7}$	b
$\mathcal{B}(B^+ \rightarrow K^+ \mu^+ e^-)$	$< 9.1 \times 10^{-8}$	b

details in [talk of Giovanni Marchiori](#)

LFV energy scale

$\Lambda_{\bar{b}d} :$

2.2 TeV \rightarrow 11 TeV

$\Lambda_{\bar{b}s} :$

2.6 TeV \rightarrow 15 TeV

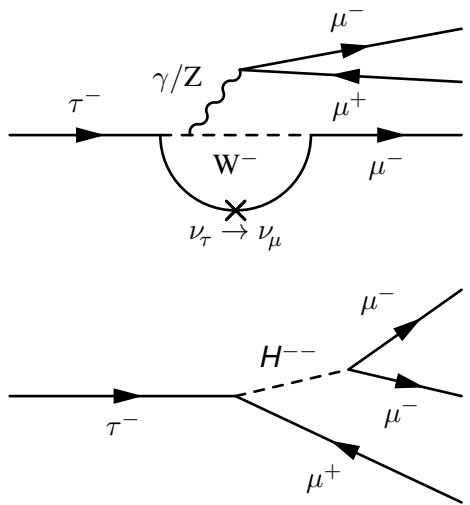
a: BaBar, [arXiv:1204.2852](#), 429 fb $^{-1}$

b: BaBar, [Phys. Rev. Let. 99, 051801 \(2007\)](#), 209 fb $^{-1}$



$\tau^- \rightarrow \mu^- \mu^- \mu^+$ at hadron colliders

- in Standard Model + neutrino oscillation introduced in penguin diagrams
- highly suppressed ($\mathcal{B} \ll 10^{-50}$)
- enhanced by e.g. charged Higgs
- best measurements conducted at B factories ([Francesco Renga's talk](#))
- ! also possible at hadron colliders





$\tau \rightarrow \mu\mu\mu$ in hadron collisions

τ sources at B factories

- $e^+e^- \rightarrow \tau^+\tau^-$
- allows τ tag

τ sources at the LHC

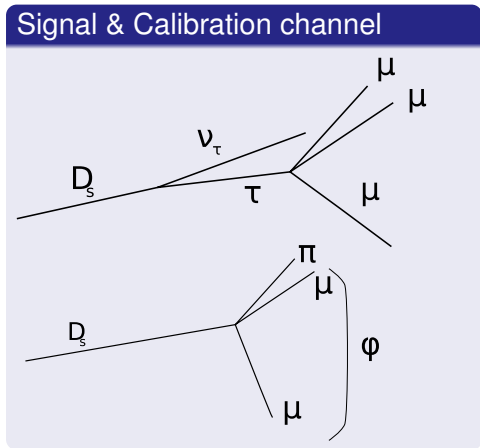
- inclusive τ cross section $79.5 \pm 8.3 \mu\text{b}$ at $\sqrt{s} = 7 \text{ TeV}$ in the LHCb acceptance
- $7.9 \times 10^{10} \tau$ produced
- dominant: $D_s \rightarrow \tau \nu_\tau$ (78%)
- ! no τ tag possible
- standard τ signatures very similar to D decays
 $(D^+ \rightarrow \pi^+\pi^-\pi^+\pi^0$
vs. $\tau^+ \rightarrow \pi^+\pi^-\pi^+\bar{\nu}_\tau)$



Strategy



- Loose cut based selection
- Classification in 3D space:
 - invariant mass
 - decay topology (multivariate)
 - particle identification (multivariate)
- Classifier trained on simulation
- Calibration with control channel
- Normalisation with D_s
- CLs method to extract the result



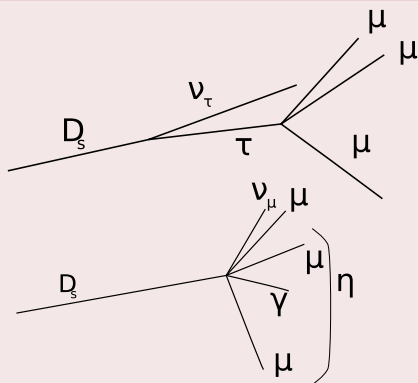


Strategy

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Signal & peaking background





Normalisation channel $D_s^+ \rightarrow \phi(\mu^+ \mu^-)\pi^+$

produced τ leptons

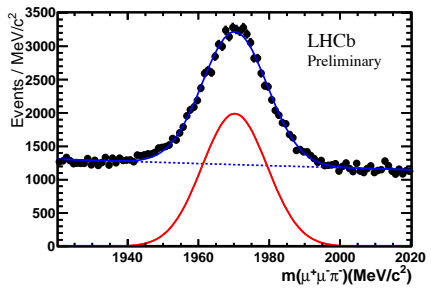
$$\mathcal{B}(\tau \rightarrow \mu\mu\mu) = \frac{\sigma(pp \rightarrow D_s \rightarrow \tau)}{\sigma(pp \rightarrow \tau)} \frac{\mathcal{B}(D_s \rightarrow \phi(\mu\mu)\pi)}{\mathcal{B}(D_s \rightarrow \tau\nu_\tau)} \frac{\epsilon_{norm}}{\epsilon_{sig}} \frac{N_{\tau \rightarrow \mu\mu\mu}}{N_{D_s \rightarrow \phi(\mu\mu)\pi}}$$

ingredients

- $b\bar{b}$ and $c\bar{c}$ production measurements from LHCb
- $B \rightarrow \tau$ and $D \rightarrow \tau$ branching ratios from LEP / B factories
- $\mu\mu\pi$ final state
- systematics cancel
 - trigger
 - reconstruction
 - selection



LHCb-CONF-2012-015



45 515 $D_s \rightarrow \phi(\mu^+ \mu^-)\pi$ decays





Normalisation channel $D_s^+ \rightarrow \phi(\mu^+ \mu^-)\pi^+$

produced τ leptons

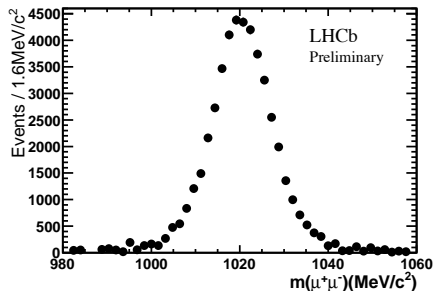
$$\mathcal{B}(\tau \rightarrow \mu\mu\mu) = \frac{\sigma(pp \rightarrow D_s \rightarrow \tau)}{\sigma(pp \rightarrow \tau)} \frac{\mathcal{B}(D_s \rightarrow \phi(\mu\mu)\pi)}{\mathcal{B}(D_s \rightarrow \tau\nu_\tau)} \frac{\epsilon_{norm}}{\epsilon_{sig}} \frac{N_{\tau \rightarrow \mu\mu\mu}}{N_{D_s \rightarrow \phi(\mu\mu)\pi}}$$

ingredients

- $b\bar{b}$ and $c\bar{c}$ production measurements from LHCb
- $B \rightarrow \tau$ and $D \rightarrow \tau$ branching ratios from LEP / B factories
- $\mu\mu\pi$ final state
- systematics cancel
- non resonant contribution < 2%



LHCb-CONF-2012-015



background subtracted $\mu^+ \mu^-$ mass





signal likelihoods

3 body decay likelihood

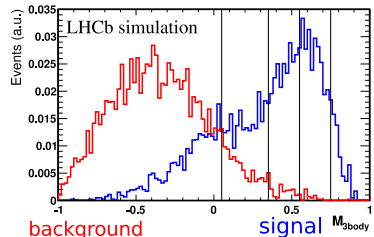
- vertex properties
 - vertex fit, pointing
- track quality
- isolation

particle identification

- hits in muon chambers
- energy in calorimeters
 - compatible with MIP
- RICH information

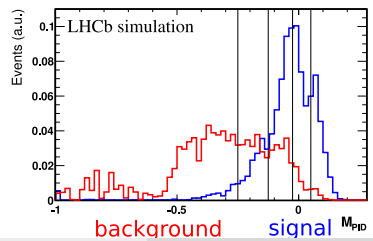
Calibration

$$D_s \rightarrow \phi \pi$$



Calibration

$$J/\psi \rightarrow \mu^+ \mu^-$$





invariant mass

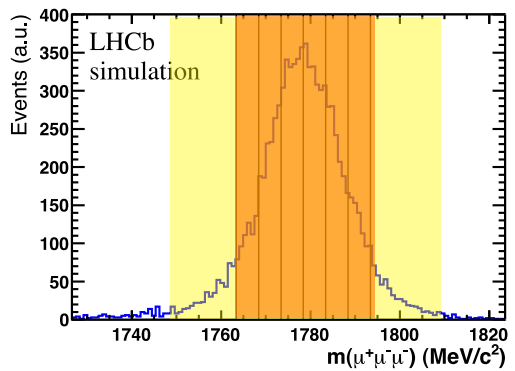
two fold role

- background estimation in sidebands
- different signal likelihood inside signal region



1 fb⁻¹

LHCb-CONF-
2012-015



- mass resolution and mass scale calibrated on data



signal likelihoods

combined signal distribution

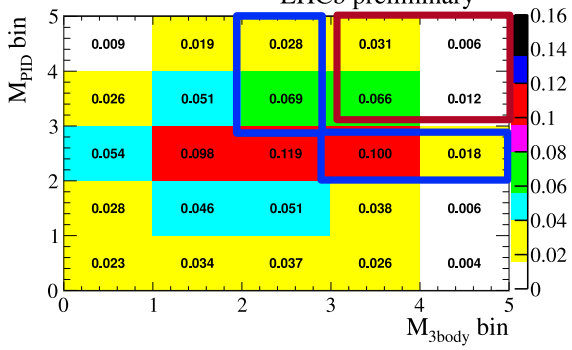
- events distributed over 25 likelihood bins
- background estimate from mass sidebands



1 fb⁻¹

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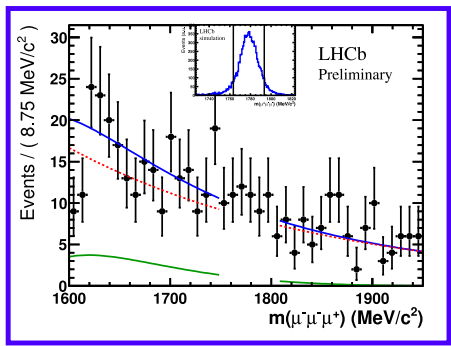
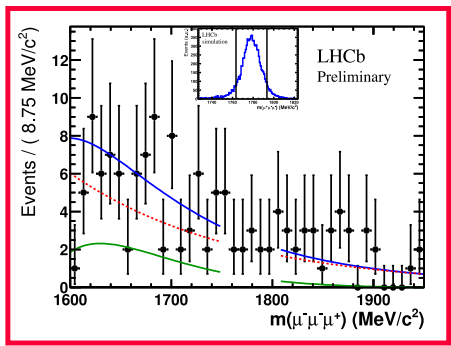
LHCb preliminary



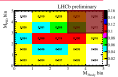
- 11 % signal efficiency
- 21 % signal efficiency
- for illustration: high likelihood range shown



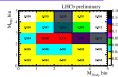
observed events



11 % of the signal
0.03 % of the background



21 % of the signal
0.14 % of the background



- red dashed combinatorial background
- green $D_s^+ \rightarrow \eta(\mu^- \mu^+ \gamma) \mu^+ \nu_\mu$
- blue combined background



1 fb⁻¹

LHCb-CONF-2012-015




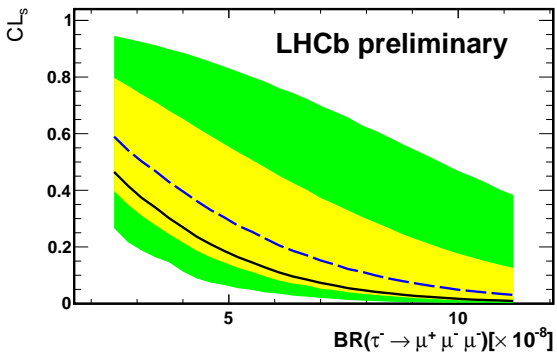


extracted limit

result (preliminary)

	observed	expected
$\mathcal{B}(\tau \rightarrow \mu\mu\mu) < 6.3 \times 10^{-8}$		8.2×10^{-8} @ 90% CL
$< 7.8 \times 10^{-8}$		9.9×10^{-8} @ 95% CL

LHCb
 1 fb⁻¹
 LHCb-CONF-
 2012-015



Belle 2.1×10^{-8} @ 90% CL
 Phys. Lett. B **687**, 139
 (2010)

BaBar 3.3×10^{-8} @ 90% CL
 Phys. Rev. D **81**,
 111101(R) (2010)



Summary

- neither lepton number violation nor lepton flavour violation observed (yet)
 - hadron decays provide good probes for Lepton Number & Flavour Violation
 - excellent sensitivity achieved at B factories
 - LNV and LFV excluded to 10^{-5} for D decays
 - LHCb extends knowledge on forbidden B decays
 - LNV excluded to $10^{-6 \dots -8}$
 - LHCb approaching B factories for $\tau \rightarrow \mu\mu\mu$
- ⇒ first time done at hadron colliders

BACKUP





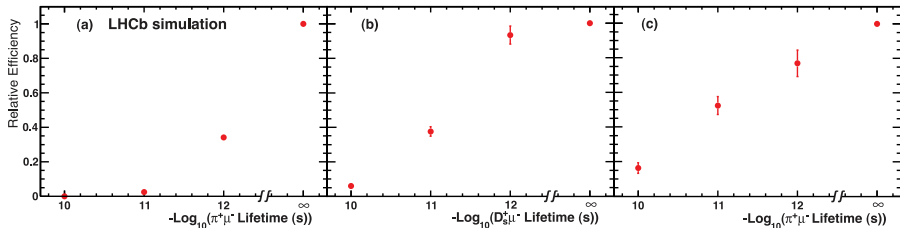
Sensitivity to long lived Majorana neutrinos

- analysis allows for neutrino flight distance
- probes only Majorana neutrinos decaying inside the detector
- sensitivity to lifetime provided

a) $B^- \rightarrow \pi^+ \mu^- \mu^-$
 $250 \text{ MeV} < m_4 < 5 \text{ GeV}$

b) $B^- \rightarrow D_s^+ \mu^- \mu^-$
 $2.1 \text{ GeV} < m_4 < 5.15 \text{ GeV}$

c) $B^- \rightarrow D^0 \pi^+ \mu^- \mu^-$
 $260 \text{ MeV} < m_4 < 3.3 \text{ GeV}$



- sensitive to lifetimes $< 10^{-10}$ s
- $B^- \rightarrow D^0 \pi^+ \mu^- \mu^-$ better sensitive to “large” lifetimes



model dependence

$$\tau^- \rightarrow \mu^- \mu^- \mu^+$$

possible problem

if the selection efficiency is different for various models, the limit could be higher or lower than the one we quote.

crosschecks

We tested the

- trigger efficiency
- preselection
- multivariate classifier

as a function of the invariant dimuon mass(es).

⇒ these are constant within 15%



Prospects

When will LHCb catch up with the B factories on $\tau^- \rightarrow \mu^- \mu^- \mu^+$?

short answer

not studied so far

long answer

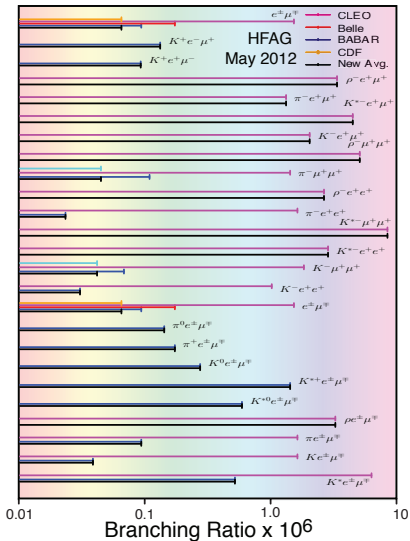
Judge yourself:

- used: 1 fb^{-1} @ 7 TeV
- 2012: 1.5 fb^{-1} @ 8 TeV (charm cross section $\sim 15\%$ higher)
- 2013-1014: long shutdown 1
- 2014-2017: running at higher energies



HFAG limits for bottom decays

Lepton Number Violating Charmless B Decays



[HFAG]