

# Search for Charged Lepton Flavour Violation at LHCb experiment

Doctoral disertation

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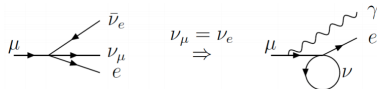


# Lepton Flavour/Number Violation

## Lepton Flavour Violation(LFV):

After  $\mu^-$  was discovered (1936) it was natural to think of it as an excited  $e^-$ .

- Expected:  $B(\mu \rightarrow e\gamma) \approx 10^{-4}$
- Unless there is a nother  $\nu$ .



I.I.Rabi:

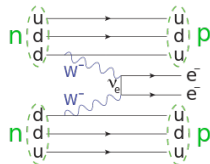
"Who ordered that?"



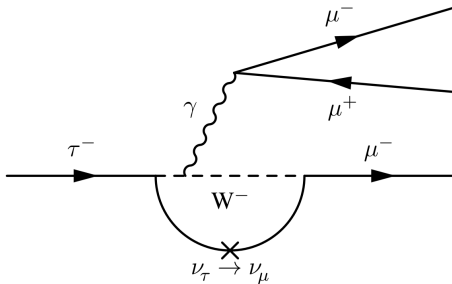
- Up to this day charged LFV is being searched for in various decay modes.
- LFV was already found in neutrino sector (oscillations).

## Lepton Number Violation (LNV)

- Even with LFV, lepton number can be a conserved quantity.
- Many NP models predict LNV (Majorana neutrinos)
- LNV searched in s-called neutrinoless double  $\beta$  decays.



# Status of searches for $\tau \rightarrow \mu\mu\mu$



- Charged Lepton Flavour Violation process.
- The Standard Model contribution: penguin diagram with neutrino oscillation

## Current limits (90% CL)

**BaBar**  $3.3 \times 10^{-8}$

**Belle**  $2.1 \times 10^{-8}$

## Predictions

**SM**  $O(10^{-40})$

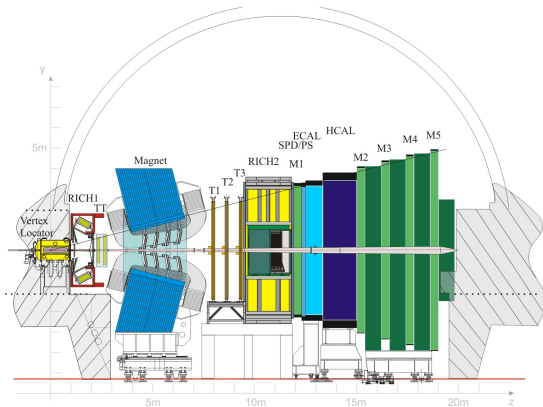
**var. SUSY**  $10^{-10}$

**non universal Z'**  $10^{-8}$

**mSUGRA+seesaw**  $10^{-9}$

**and many more...**

# LHCb detector



LHCb is a forward spectrometer:

- Excellent vertex resolution.
- Efficient trigger.
- High acceptance for  $\tau$  and B.
- Superb particle identification (PID).



- 1 Data sample:  $1\text{fb}^{-1}$  7 TeV and  $2\text{fb}^{-1}$  8TeV.
- 2 Normalization (control) decay channel:  $D_s \rightarrow \phi(\mu\mu)\pi$ .
- 3 Blind analysis.
- 4 Event selection:
  - Preselection of three tracks that combine to give a mass close to  $m_\tau$ , with displaced vertex.
  - Selection based on three classifiers:
    - Geometry and topology ( $\mathcal{M}_{3body}$ )
    - PID ( $\mathcal{M}_{PID}$ )
    - Three muon invariant mass ( $m_{\mu\mu\mu}$ )
- 5 Major background contributions:  $D_s \rightarrow \eta(\mu\mu\gamma)\mu\nu$  and  $D \rightarrow K\pi\pi$ .
- 6 Evaluation of the upper limit on  $\mathcal{B}(\tau \rightarrow \mu\mu\mu)$  using  $CL_s$ .



- $\tau$ 's in LHCb come from five main sources:

Mode	7 TeV	8 TeV
Prompt $D_s \rightarrow \tau$	$71.1 \pm 3.0\%$	$72.4 \pm 2.7\%$
Prompt $D^+ \rightarrow \tau$	$4.1 \pm 0.8\%$	$4.2 \pm 0.7\%$
Non-prompt $D_s \rightarrow \tau$	$9.0 \pm 2.0\%$	$8.5 \pm 1.7\%$
Non-prompt $D^+ \rightarrow \tau$	$0.18 \pm 0.04\%$	$0.17 \pm 0.04\%$
$X_b \rightarrow \tau$	$15.5 \pm 2.7\%$	$14.7 \pm 2.3\%$

- Pythia produces them in wrong proportions
- Channels were produced separately and added in the given proportions.

## $\mathcal{B}(D^+ \rightarrow \tau)$

- There is no measurement of  $\mathcal{B}(D^+ \rightarrow \tau)$ .
- One can calculate it from:  $\mathcal{B}(D^+ \rightarrow \mu\nu_\mu)$  + helicity suppression + phase space, hep-ex:0604043.
- $\mathcal{B}(D^+ \rightarrow \tau\nu_\tau) = (1.0 \pm 0.1) \times 10^{-3}$ .



# Triggers at LHCb

- LHCb uses complex trigger,  $\mathcal{O}(100)$  trigger lines.
- Lines change with data taking.
- Optimized choice of triggers based on  $\frac{s}{\sqrt{b}}$  FOM,

$$\epsilon(\beta)'_{\text{evt,line}} = \frac{N(\tau \text{ MC(BKG) events triggered line, but not by any better line})}{N(\tau \text{ MC(BKG) events triggered by any line)},$$

- Evaluated different triggers used in 2012 data taking.
- Found negligible differences in trigger efficiencies.

$$\text{CTFM} = \frac{\sqrt{\sum_{\text{trigger lines}} \beta'_{\text{evt,line}}}}{\sum_{\text{trigger lines}} \epsilon'_{\text{evt,line}}}$$

name	$\epsilon'$	$\beta'$	CTFM
Hlt2TriMuonTauDecision	0.880708	0.736182	0.974228
Hlt2DiMuonDetachedDecision	0.0669841	0.173396	1.00636
Hlt2CharmSemilep3bodyD2KMuMuDecision	0.0206816	0.0182935	0.99472
Hlt2CharmHadD2HHHDecision	0.00554351	0.00666405	0.992604
Hlt2CharmSemilep3bodyD2KMuMuSSDecision	0.00195444	0.00470404	0.993106
Hlt2CharmSemilep3bodyD2PiMuMuDecision	0.00206105	0.00679472	0.994591
Hlt2TopoMu3BodyBBBDTDecision	0.00394442	0.0121521	0.996937





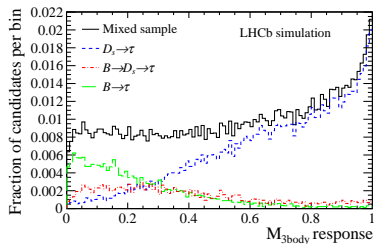
- As mentioned in LHC we have different production sources of  $\tau$ 's.
- Each source has different detector response signature.
- To maximise our performance we trained classifiers for each of the  $\tau$  sources using:
  - Kinematic properties of  $\tau$  candidate.
  - Geometric properties of  $\tau$  candidate, like pointing angle, DOCA, Vertex  $\chi^2$ , flight distance.
  - Isolations, for vertex and individual tracks.
- After training the individual classifiers one that combines all this information in a single classifier on mixed sample of  $\tau$ 's.
- This technique is known as Blending or Ensemble learning.
- Using this approach we gain 6% sensitivity!



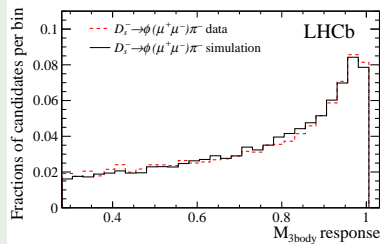
# Performance of Blend classifier

- Classifier prefers  $\tau$ 's from prompt  $D_s$ , the dominant channel.

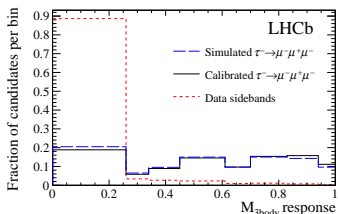
## MC response for different $\tau$ production channels



## Response for $D_s \rightarrow \phi\pi$ data and MC



- Assume all differences between  $\tau \rightarrow \mu\mu\mu$  and  $D_s \rightarrow \phi\pi$  come from kinematics (mass, resonance, decay time), which is correct in MC.
- Get correction  $D_s \rightsquigarrow \tau$  from MC.
- Apply corrections to  $D_s \rightarrow \phi\pi$  on data.

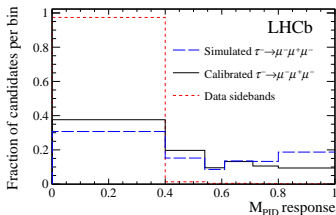


- $D_s \rightarrow \phi\pi$  well modelled in MC.



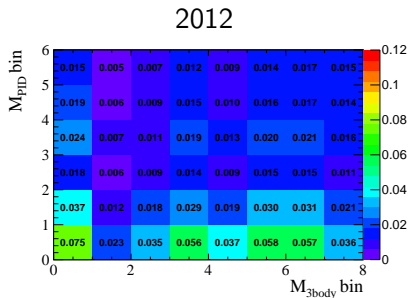
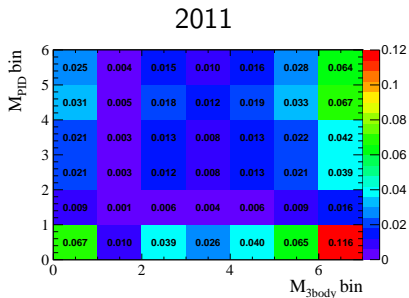
# Particle Identification (PID)

- Classifier trained on inclusive MC sample.
- Using information from: RICH, Calorimeters, Muon system and tracking.
- Correct for the MC efficiency using control channel:  
 $D_s \rightarrow \phi(\mu\mu)\pi$  and  $B \rightarrow J/\psi(\mu\mu)K$



# Binning optimisation

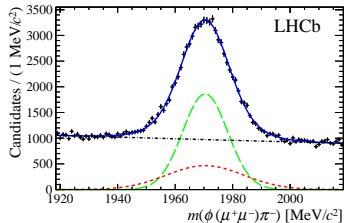
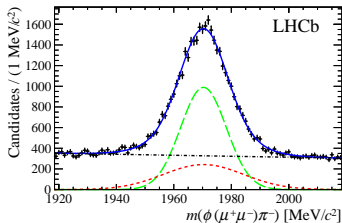
- Events are distributed among  $\mathcal{M}_{3body}, \mathcal{M}_{PID}$  plane.
- In 2D we group the events in groups(bins)
- Bins are optimised using  $CL_s$  method.
- The lowest bins are rejected, because they do not contribute to the limit sensitivity.
- In rest of the bins a fit to mass side-bands is performed in order to estimate number of expected background in signal window.



# Mass shape

- Double-Gaussian with fixed fraction (70 % inner Gaussian).
- Fix fraction to ease calibration.
- Correct mass by MC:

$$\sigma_{data}^{\tau} = \frac{\sigma_{MC}^{\tau}}{\sigma_{MC}^{D_s}} \times \sigma_{data}^{D_s}$$



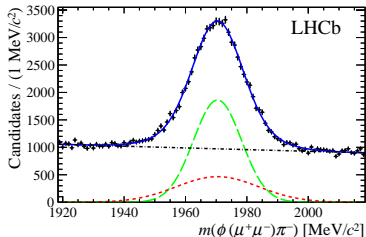
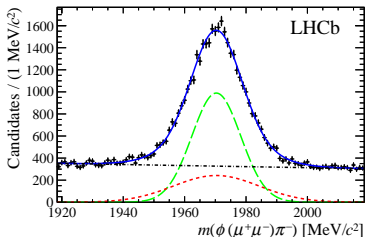
Calibrated $\tau$ Mass shape	7 TeV	8 TeV
Mean (MeV)	$1779.1 \pm 0.1$	$1779.0 \pm 0.1$
$\sigma_1$ (MeV)	$7.7 \pm 0.1$	$7.6 \pm 0.1$
$\sigma_2$ (MeV)	$12.0 \pm 0.8$	$11.5 \pm 0.5$



# Relative normalisation

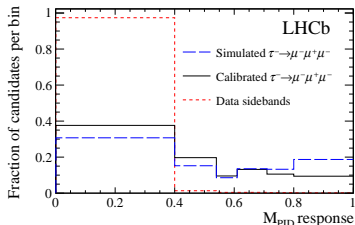
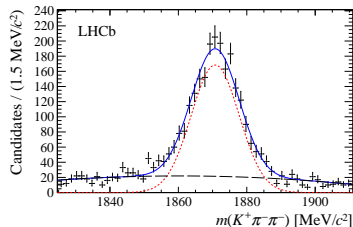
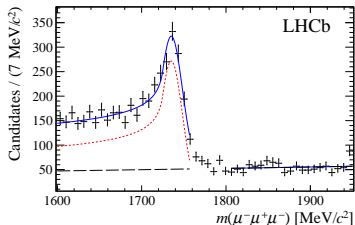
$$\mathcal{B}(\tau \rightarrow \mu\mu\mu) = \frac{\mathcal{B}(D_s \rightarrow \phi\pi)}{\mathcal{B}(D_s \rightarrow \tau\nu_\tau)} \times f_{D_s}^\tau \times \frac{\varepsilon_{\text{norm}}}{\varepsilon_{\text{sig}}} \times \frac{N_{\text{sig}}}{N_{\text{norm}}} = \alpha \times N_{\text{sig}}$$

- where  $\varepsilon$  stands for trigger, reconstruction, selection efficiency.
- $f_{D_s}^\tau$  is the fraction of  $\tau$  coming from  $D_s$ .
- norm = normalisation channel  $D_s \rightarrow \phi\pi$   
i.e.  $(83 \pm 3)\%$  for 2012.



# Misidentification

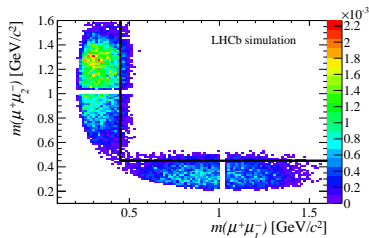
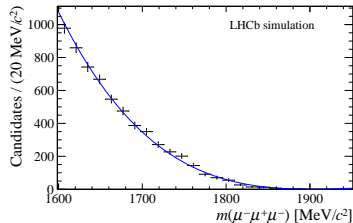
- Most dominant:  $D^+ \rightarrow K\pi\pi$ .
- Also seen  $D^+ \rightarrow \pi\pi\pi$  and  $D_s \rightarrow \pi\pi\pi$ .
- All contained in the lowest  $\mathcal{M}_{PID}$  bin.





# Dangerous backgrounds

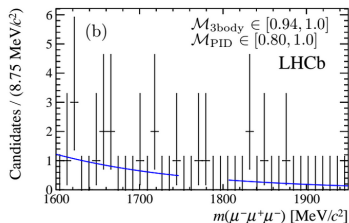
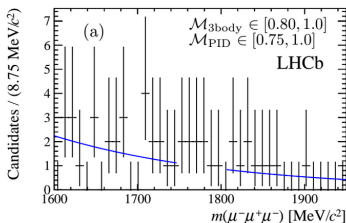
- $\phi \rightarrow \mu\mu + X$ : narrow veto on dimuon mass.
- $D_s \rightarrow \eta(\mu\mu\gamma)\mu\nu_\mu$ : not so easy:
  - Model it
  - Remove it with dimuon mass cut:
    - Fits better understood.
    - Sensitivity unchanged when removing veto.
    - Smaller uncertainty on expected background.



# Remaining backgrounds

- Fit exponential to invariant mass spectrum in each likelihood bin.
  - Don't use blinded region ( $\pm 30$  MeV).
- Compatible results blinding only  $\pm 20$  MeV<sup>1</sup>

Example of most sensitive regions in 2011 and 2012

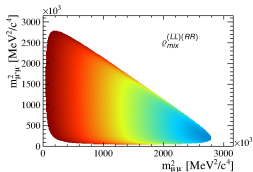
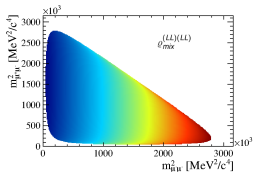
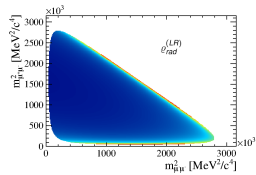
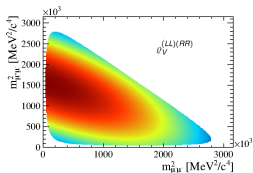
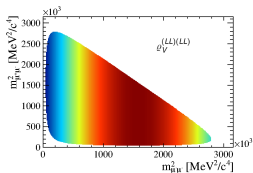


<sup>1</sup>partially used in classifier development



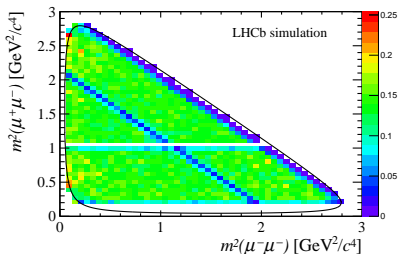
# Model dependence

- $\eta$  veto  $\Rightarrow$  our limit not constraining to New Physics with small  $m_{\mu^+\mu^-}$ .
- Model description in [arXiv:0707.0988](https://arxiv.org/abs/0707.0988) by S.Turczyk.
- 5 relevant Dalitz distributions: 2 four-point operators, 1 radiative operator, 2 interference terms.

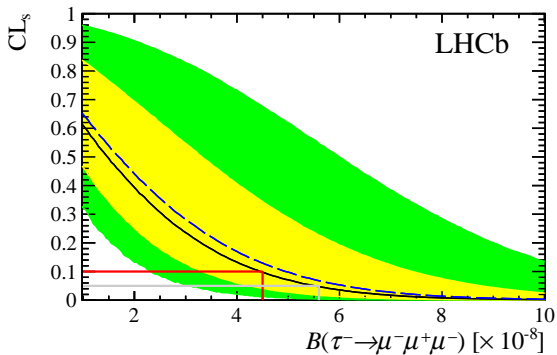


# Model dependence

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- Model description in [arXiv:0707.0988](https://arxiv.org/abs/0707.0988) by S.Turczyk.
- 5 relevant Dalitz distributions: 2 four-point operators, 1 radiative operator, 2 interference terms.
- With radiative distribution limit gets worse by a factor of 1.5 (dominantly from the  $\eta$  veto).
- The other four Dalitz distributions behave nicely (within 7 %).



# Results



Limits(PHSP):

Observed(Expected)

$4.6 (5.0) \times 10^{-8}$  at 90% CL

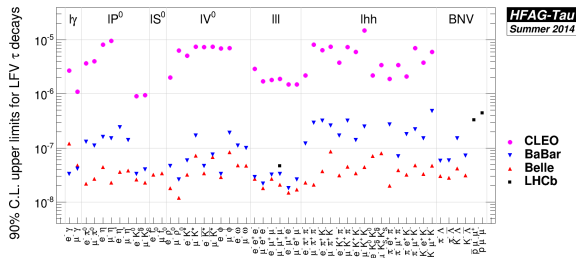
$5.6 (6.1) \times 10^{-8}$  at 95% CL

Dalitz distribution	$\times 10^{-8}$
$\varrho_V^{(LL)(LL)}$	4.2 (4.7)
$\varrho_V^{(LL)(RR)}$	4.1 (4.6)
$\varrho_V^{(LR)}$	6.8 (7.6)
$\varrho_{rad}^{(LL)(LL)}$	4.4 (5.1)
$\varrho_{mix}^{(LL)(RR)}$	4.6 (5.0)
$\varrho_{mix}$	



# Combination of LFV UL 1/2

- Searches for LFV in  $\tau$  sector is a domain of B factories.
- Over last years both BaBar and Belle set very strong limits on branching fractions of several rare  $\tau$  decays.



- Since those limits are used to constraint NP models, their "official" combination is of paramount importance.
- Various methods of limit computation used in Belle and BaBar's studies.
- The HFAQ group recomputed consistently all estimates using the  $CL_s$  method and the the same approach was involved in the average evaluation.





# "The Rule of Three"

## $\tau \rightarrow \mu\mu\mu$ limits (90% CL)

**BaBar(FC)**  $3.3 \times 10^{-8}$

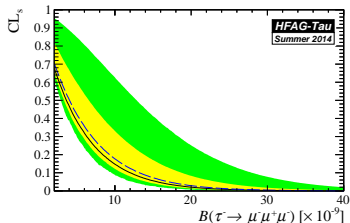
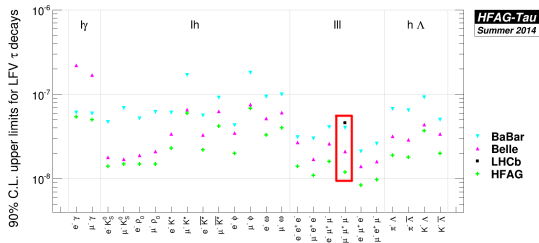
**Belle(FC)**  $2.1 \times 10^{-8}$

**LHCb(CLs)**  $4.6 \times 10^{-8}$

**HFAG(CLs)**  $1.2 \times 10^{-8}$

To conclude:

- LHCb is reaching B-factories limits.
- Many new techniques developed to perform this analysis.
- Combination of UL within HFAG gave the best sensitivity for  $\mathcal{B}(\tau \rightarrow \mu\mu\mu) < 1.2 \times 10^{-8}$  at 90% CL.





# Backup



- ① Podrozdział (4.10) ten jest de facto zapowiedzią większej pracy. Szkoda, że materiał tu przedstawiony potraktowany został bardzo skrótowo, co wymusiło na mnie konieczność kilkakrotnego przeczytania tego podrozdziału i utrudniło docenienie wyniku otrzymanego przez autora w konfrontacji z przewidywaniami teoretycznymi.
- The theory part of this was presented in detail in 2.3.4. This chapter is just a showing how to reweight the distributions to a given NP model, thats why I tried to keep it short, but I agree I over did it.



- ① Jedyne rzucające się w oczy uchybienie redakcyjne to pomyłki w numerach rozdziałów, których zawartość wymieniona jest pod koniec Wstępu.
- Mea Cupla. Completely missed that.

